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SICK
Sensor Intelligence.

: Sub-Nyquist Sampling for TDR Sensors:

Finite Rate of Innovation with Dithering

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Who We are



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- : Introduction – TDR Sensor
- : Problem Formulation
- : FRI and the Proposed Approach
- : Description of the System
- : Simulations
- : Conclusion

Time Domain Reflectometry Sensor (Guided Wave Radar Level Sensor)

Aim: to measure liquid level in an industrial container by measuring ToF.

Reflection coefficient:

$$R = \frac{Z_1 - Z_0}{Z_1 + Z_0}$$

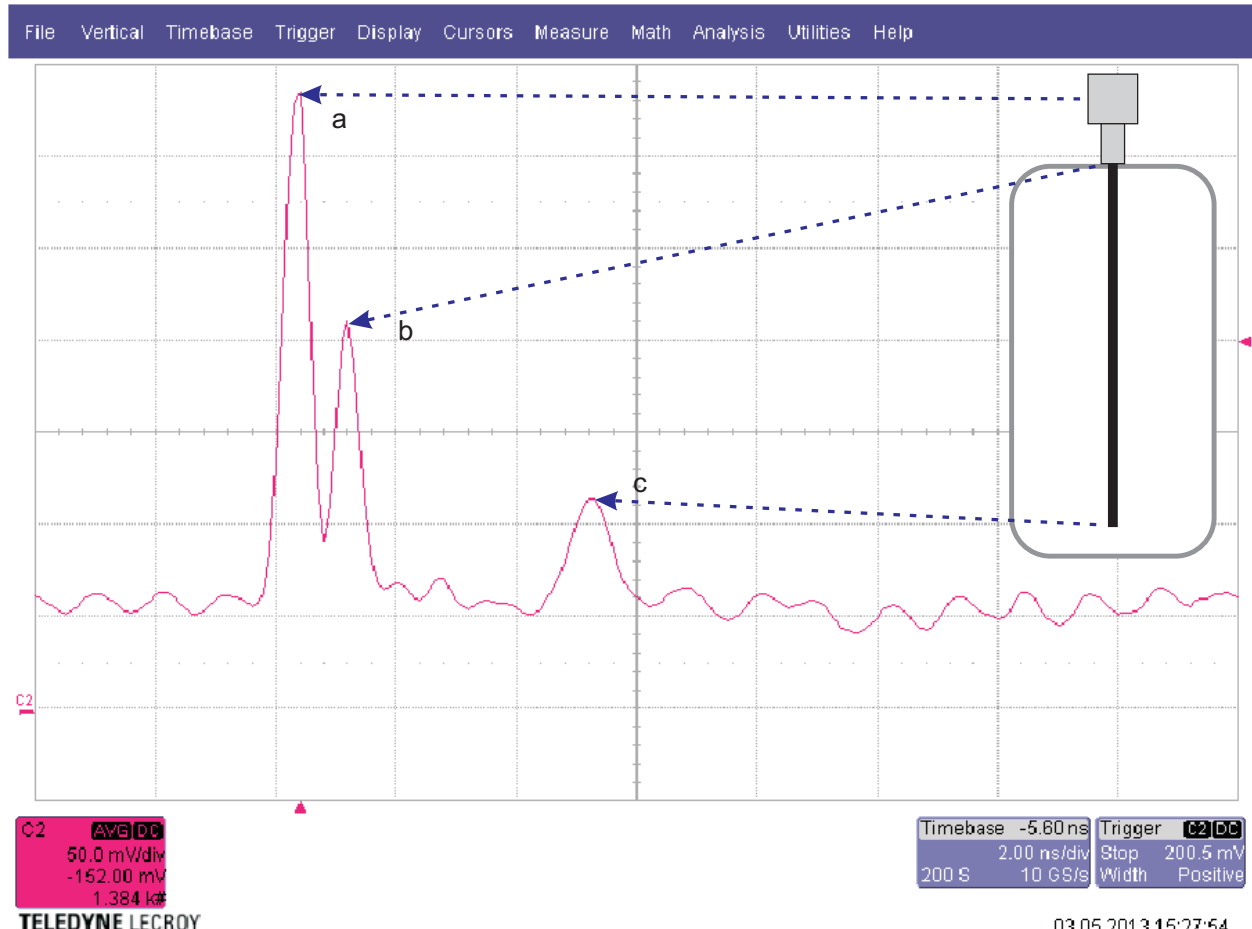
The processed signal (K pulses):

$$x(t) = \sum_{i=0}^{K-1} a_i p(t - t_i)$$

a_i : amplitude of the reflected pulse.

t_i : location of the reflected pulse.

Gaussian pulses are typically used with given σ values.



Sensing requirements:

Requirement	Value
Measuring Range	5 cm ... 10 m
Inaccuracy	< 5mm
Resolution	< 0.5 mm
Response Time	< 100 ms

➔ Maximum tolerated relative ToF measurement error is:

$$t_{\text{error}} = \frac{s}{c} = 33 \text{ ps}$$

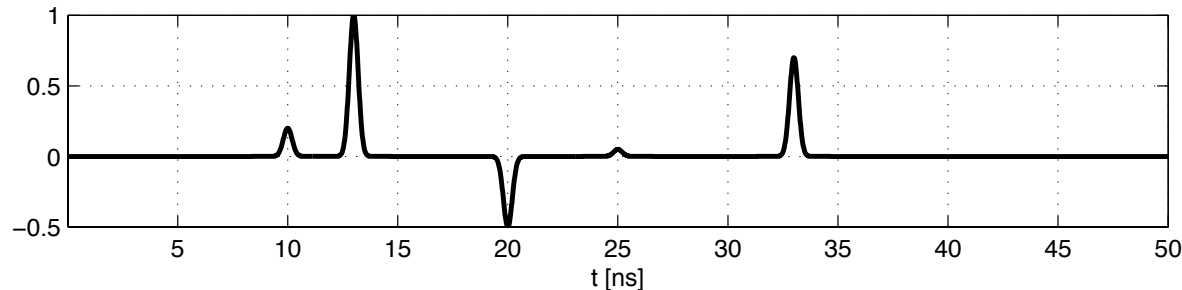
TDR-Level Sensor
LFP Cubic; SICK AG



Problem Formulation and Proposed Approach

Classical Nyquist sampling demands collecting several Giga samples per second.

- Infeasible due to practical SWPaC limitations of miniature TDR sensors.



Alternative sub-Nyquist techniques:

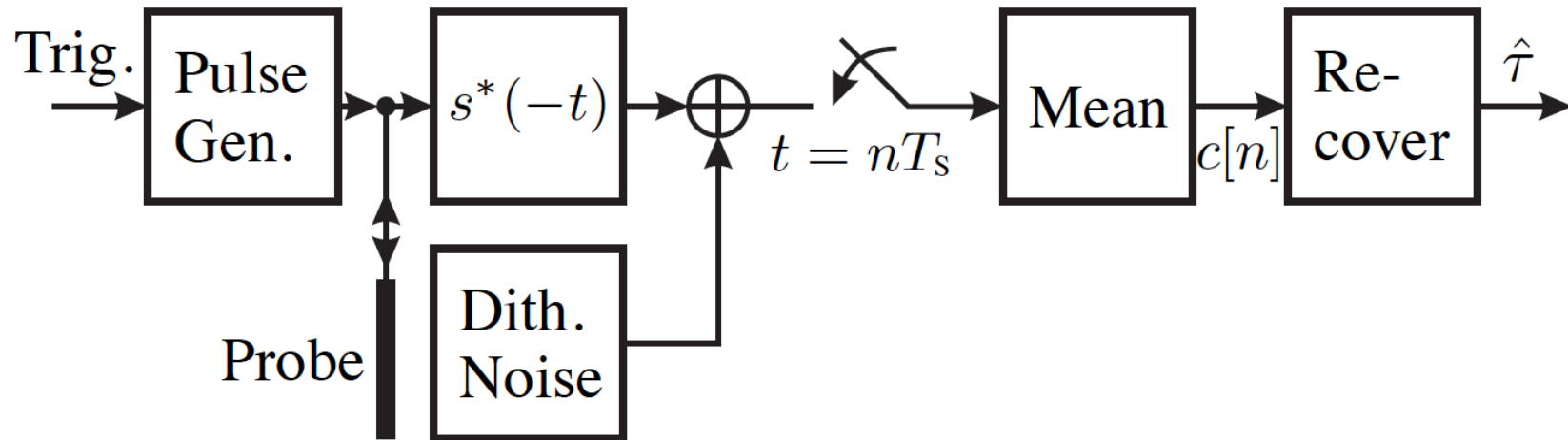
- **Equivalent Time Sampling:** Bulky sensitive circuits (PLL) and long signal acquisition times.
- **Compressed Sensing:** Infinite time resolution and high SWPaC implementation.
- **Finite Rate of Innovation:** Can be easily integrated into existing TDR sensor architecture.

FRI is an effective solution to the data acquisition problem in TDR sensors.

FRI Limitation: Very sensitive to quantisation noise and high resolution ADCs cannot be used, e.g. due to TDR sensor practical limitations.

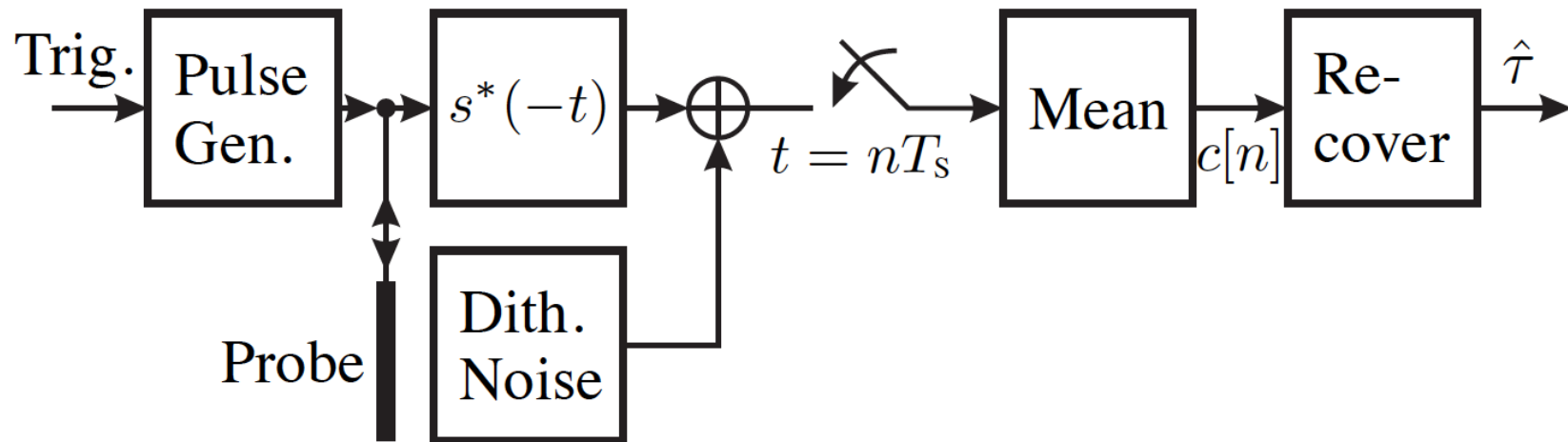
Proposed Approach: FRI with dithering and averaging to combat quantisation noise.

Implementation using FRI with Dithering and Averaging



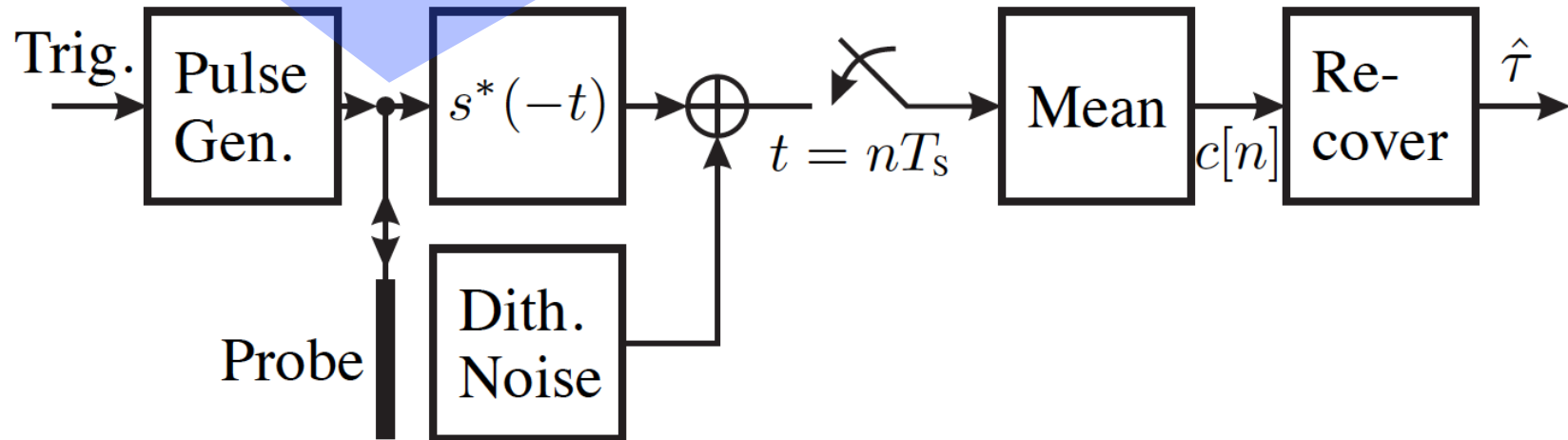
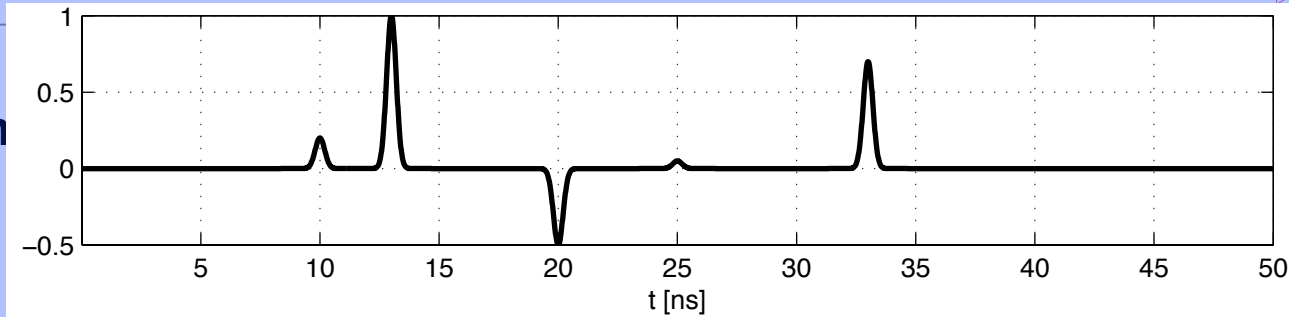
- : Ensemble averaging of consecutive sequences shall improve the ADC resolution.
- : Averaging may lead to a slightly increased response time.

Signals along the path



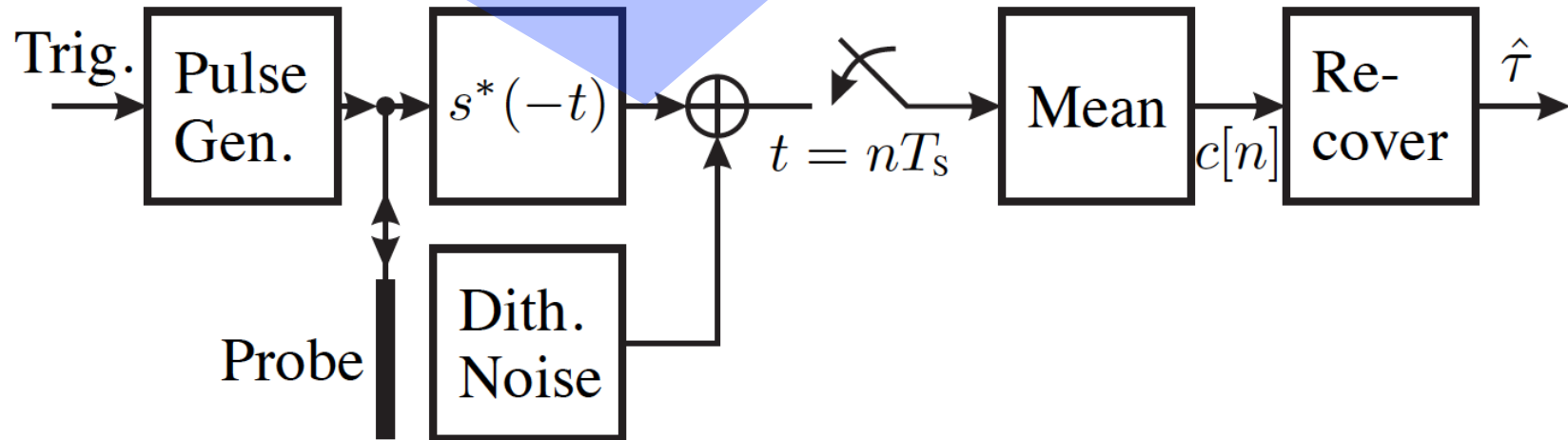
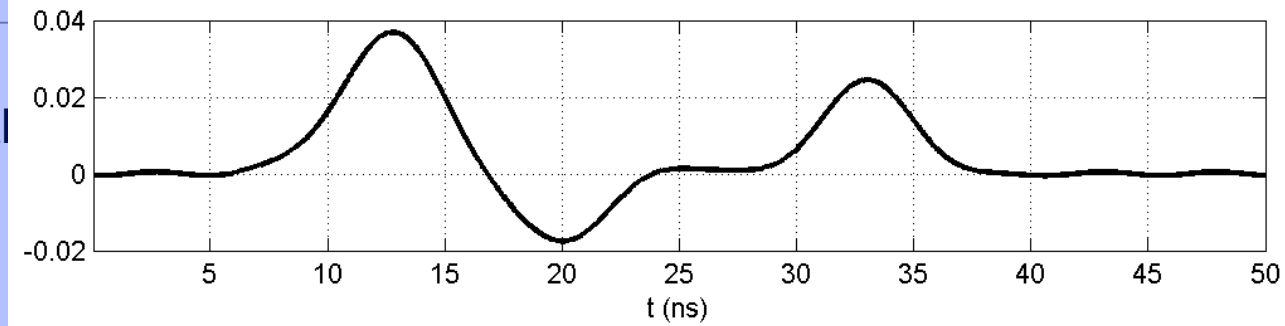
Description of the System

Signals along



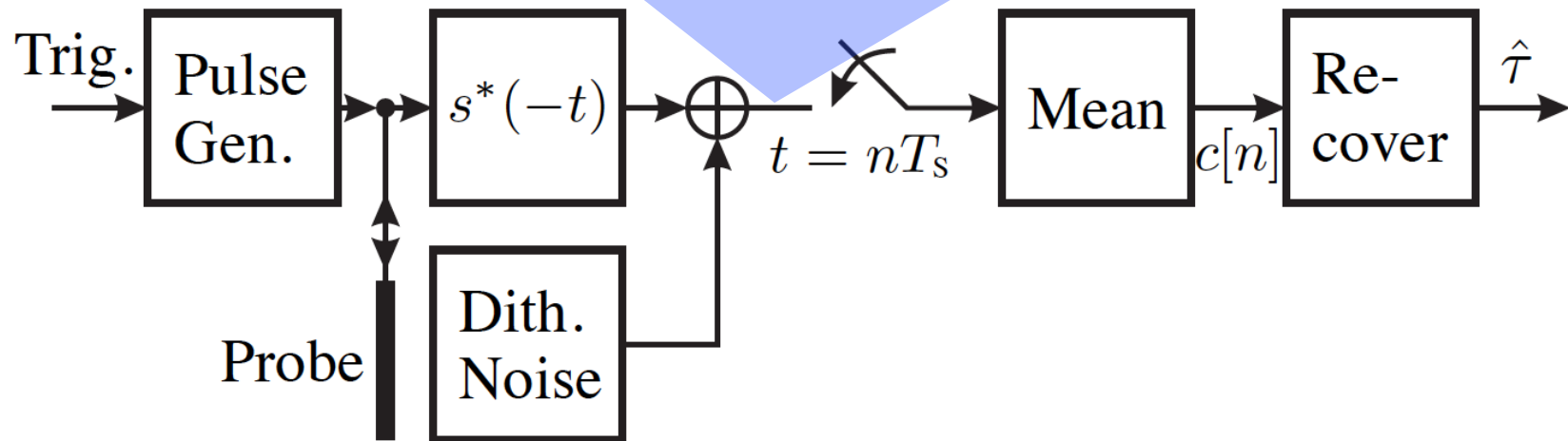
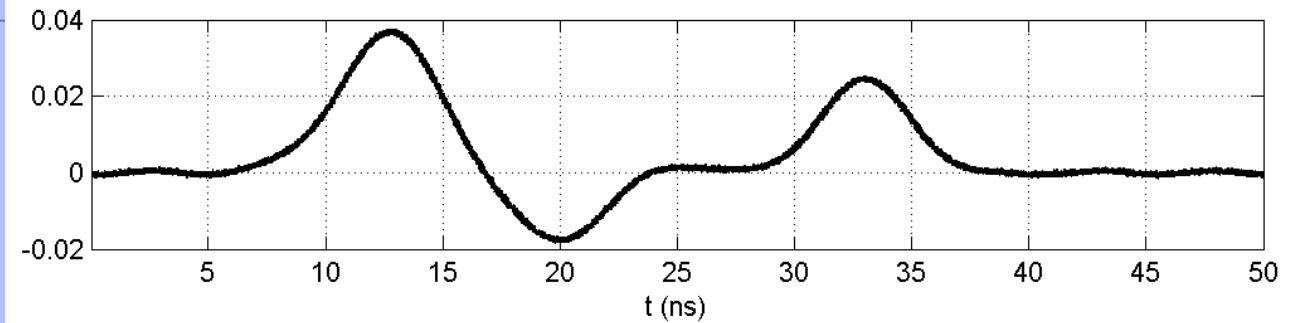
Description of the System

Signals along the path

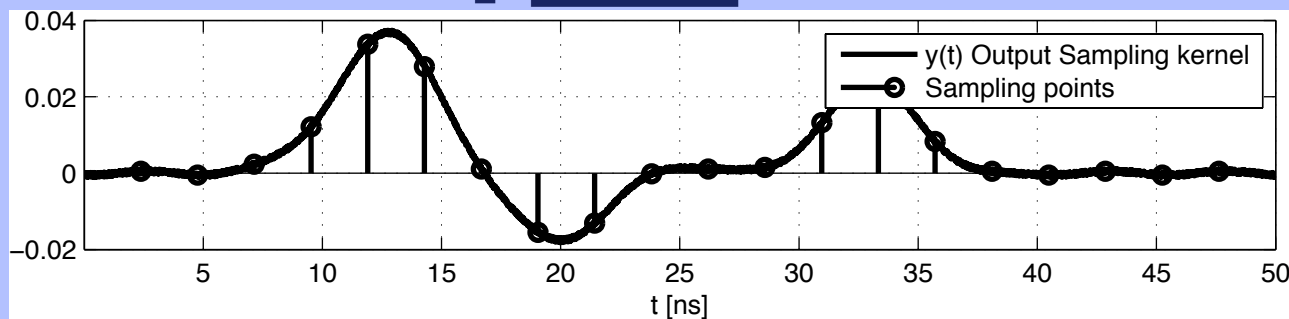
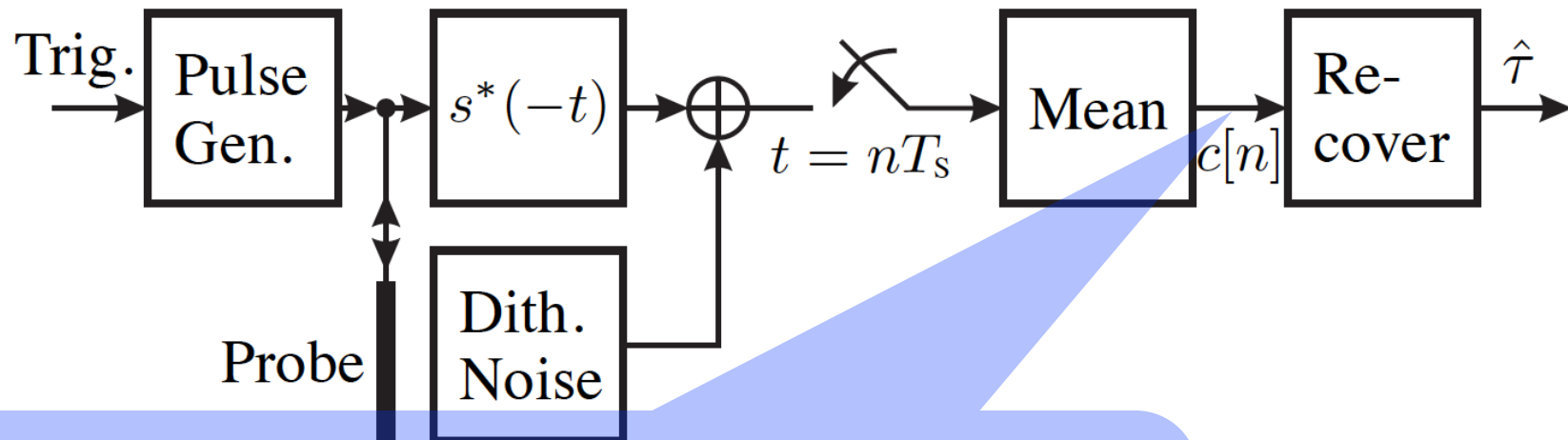


Description of the System

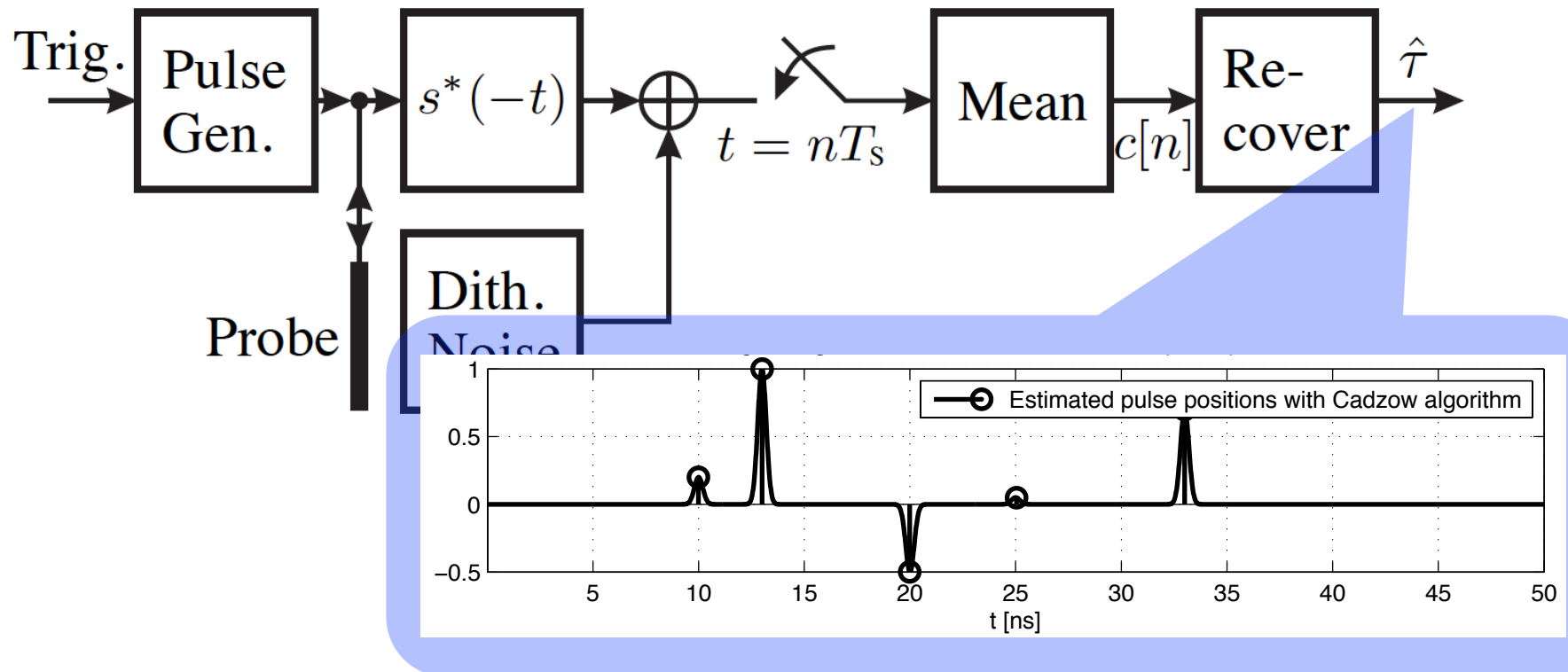
Signals along the path



Signals along the path

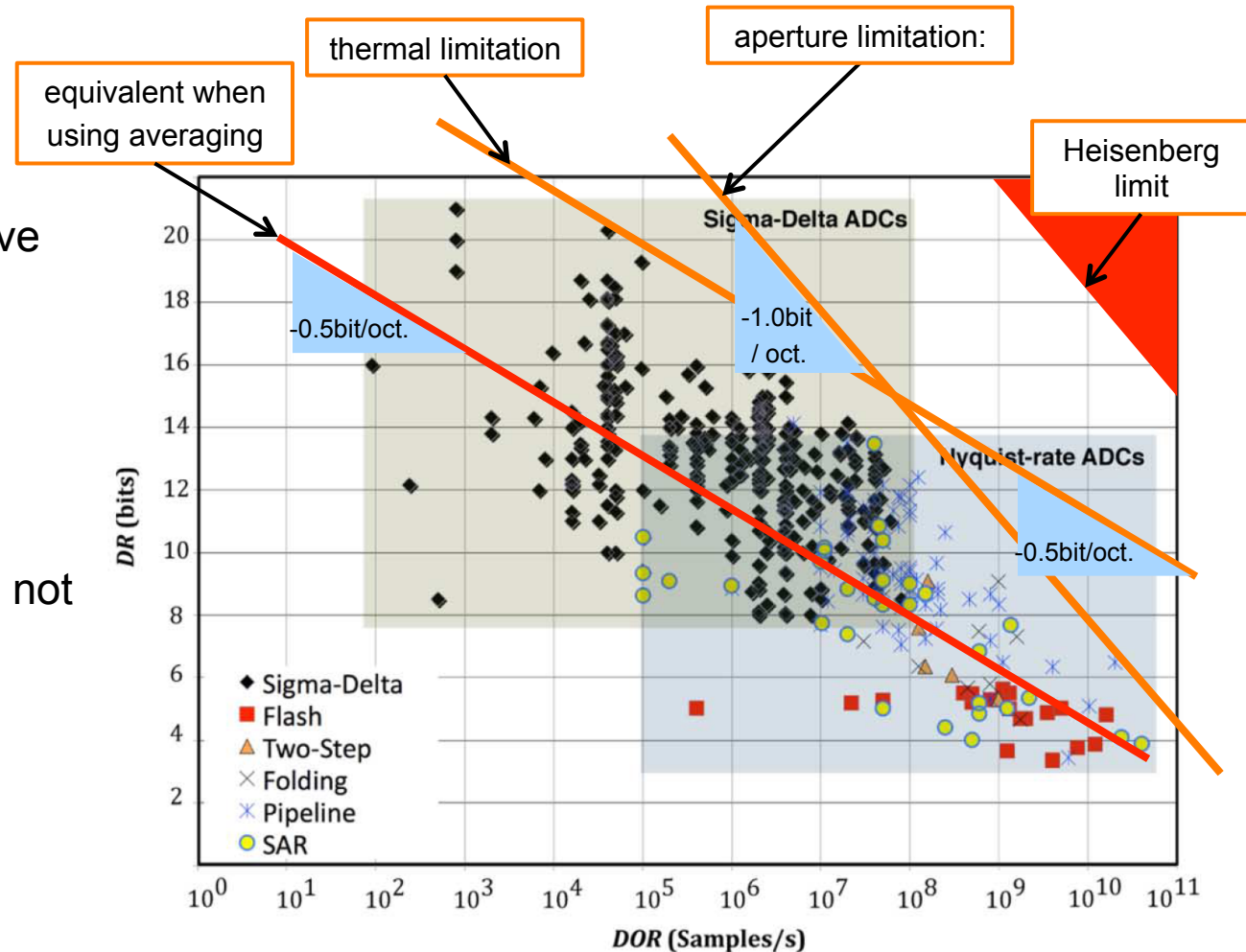


Signals along the path



ADC selection

- Resolutions $> 8\text{bit}$ are expensive for $f_s < 1\text{ns}$.
- High-speed ADCs are mainly limited by the aperture jitter.
- Averaging adjacent samples is not efficient; ensemble averaging however is.



Graph taken from: "Sigma-Delta Modulators: Tutorial Overview, Design Guide, and State-of-the-Art Survey"; IEEE Trans. on Circuits and Systems, Vol. 58, No. 1, Jan. 2011
 Limitations according: R. H. Walden: "ADC Survey and Analysis", IEEE Journal on Selected Areas in Communications, Vol. 17, No. 4, April 1999

Signal Model:

- $K = 5$ Gaussian Pulses with $\sigma = 200$ ps, each.
- Period of the pulse sequence is 50 ns.
- Two dynamic ranges are examined: 0 dB and 26 dB.

FRI:

- Sum of Sincs (SoS) sampling kernel is used.
- Cadzow plus total least squares are applied.
- FRI minimum sampling rate is 220 MHz.

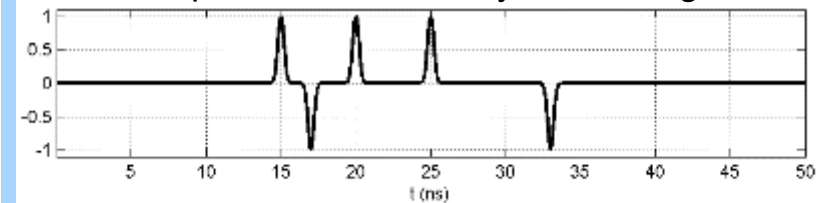
Dithering:

- Uniform distributed dither is used.
- Maximum dithering amplitude is $\pm Q/2$.

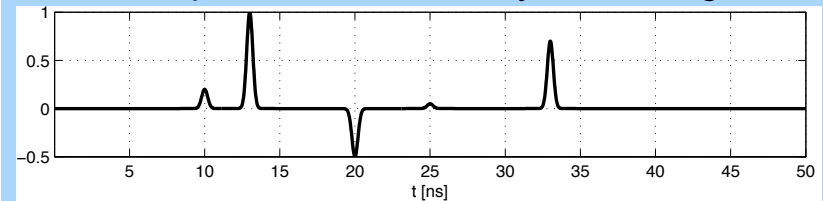
Assessment:

- Maximum error and RMS error are used to assess the results accuracy.
- In practise the maximum error is more important.

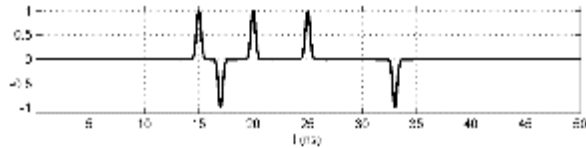
Pulse sequence with 0 dB dynamic range:



Pulse sequence with 26 dB dynamic range:

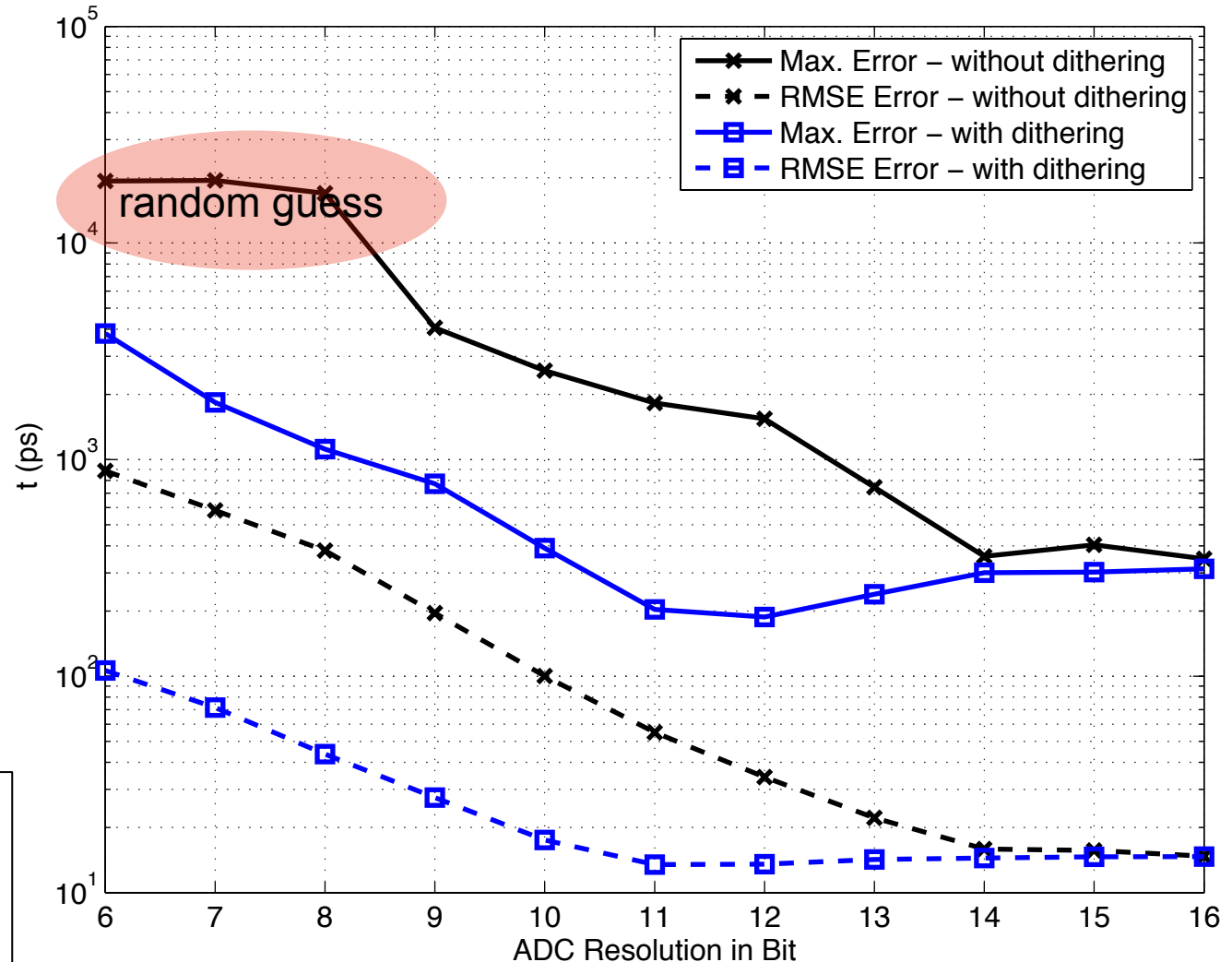


Effect of ADC Resolution



(0 dB dynamic range)

- Errors of more than 10 ns correspond to random guesses.
- ADC resolution of at least 10 bits is needed.



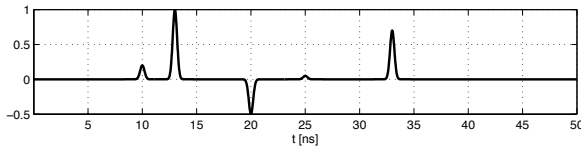
Simulation parameters:

sampling rate: $f_s = 440$ MHz

oversampling: $\beta = 2$

averaging: 250 times

Effect of ADC Resolution

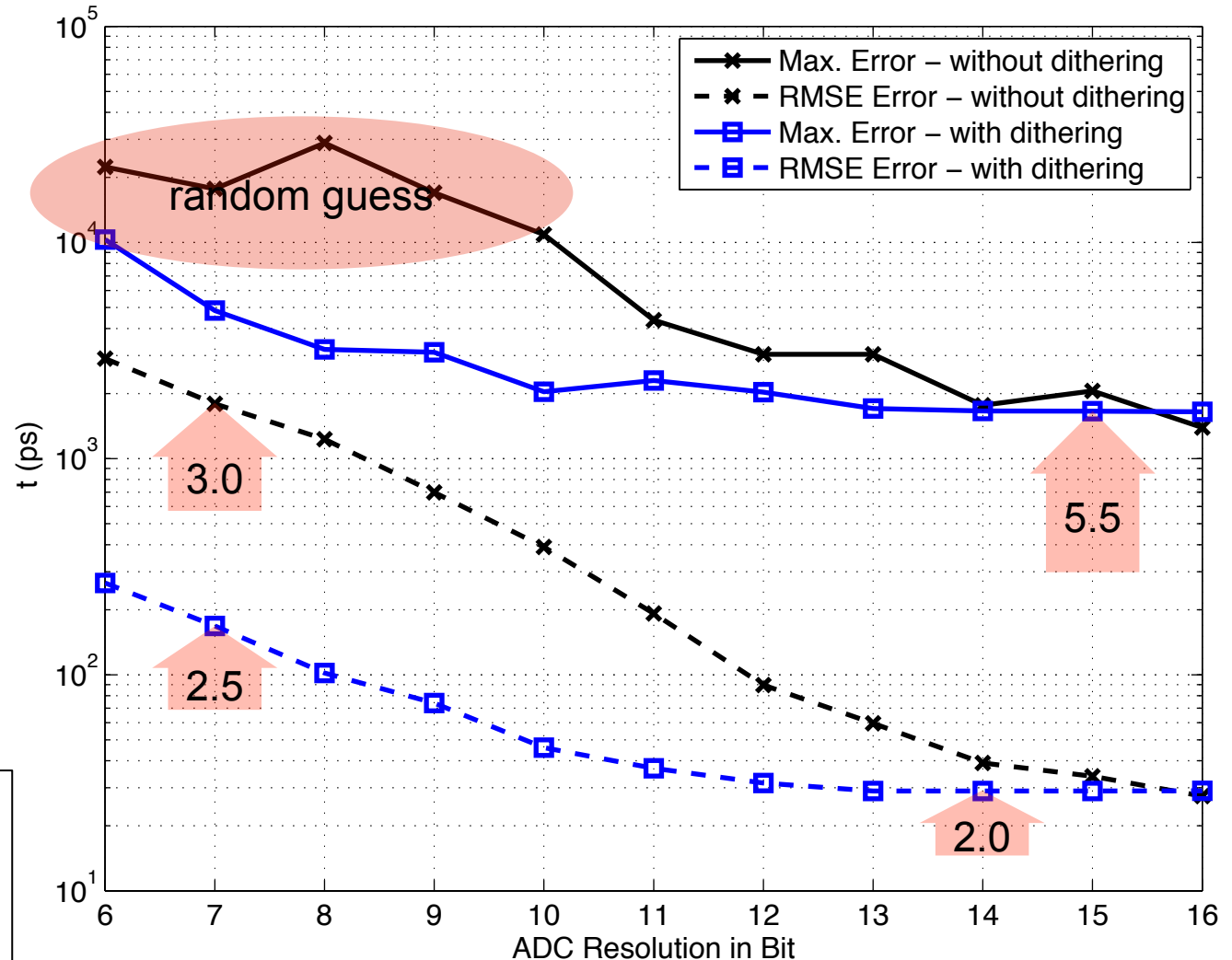


(26 dB dynamic range)

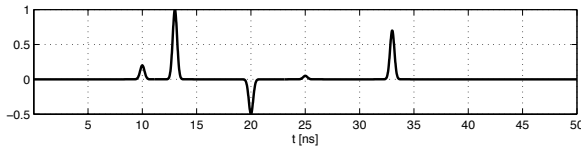
- 26 dB dynamic range causes the RMSE time resolution to decrease by a factor of 2 to 3.
- random guesses occur with ADC resolutions of up to 10 bits.
- maximum error notably increases by 5.5.

Simulation parameters:

sampling rate: $f_s = 440$ MHz
 oversampling: $\beta = 2$
 averaging: 250 times



Effect of Averaging



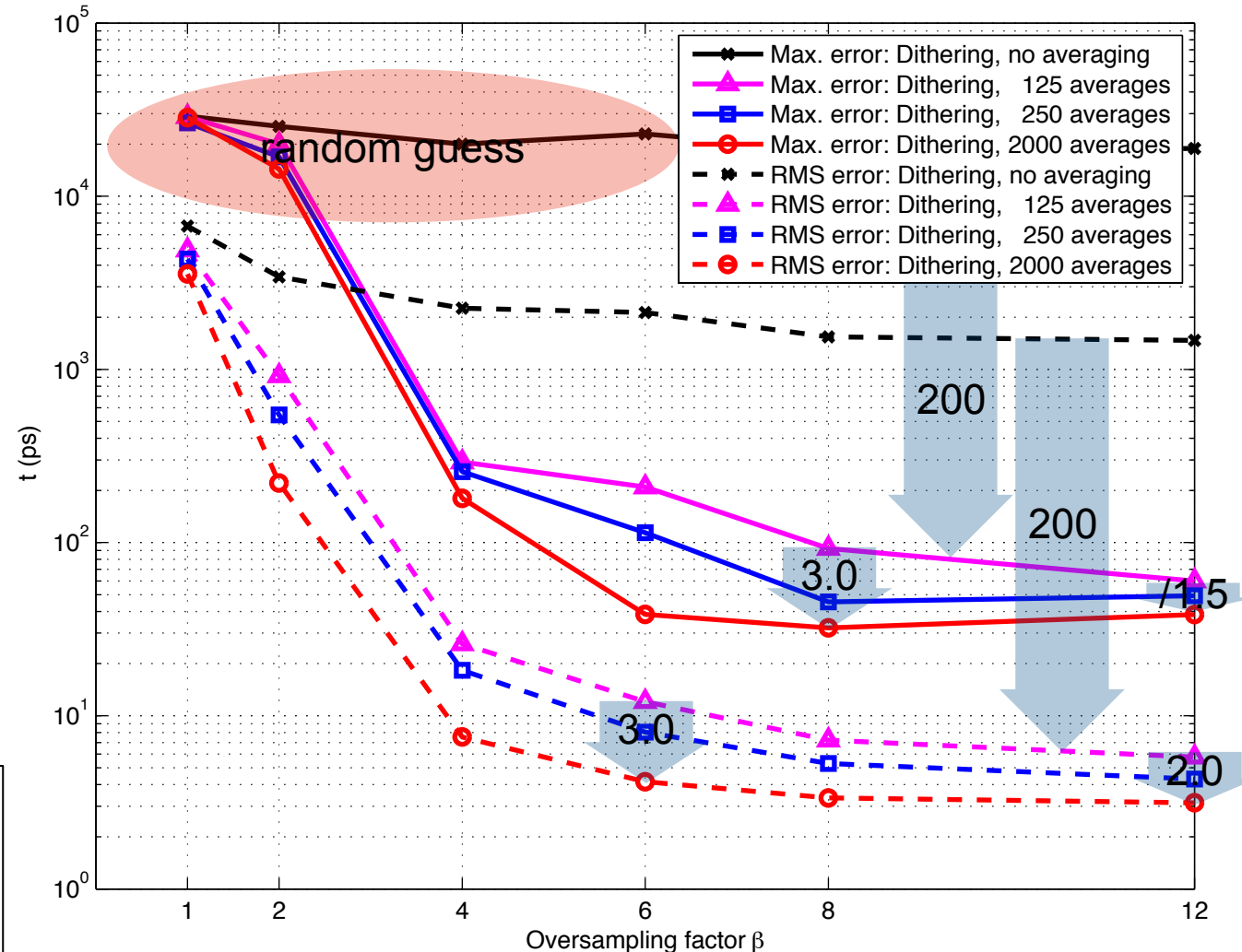
- Averaging 125 estimates enhances the RMSE time resolution by factor of 200.
- A further increase of the number of averages to 2000 enhances the RMSE time resolution again by at least a factor of 2.

Simulation parameters:

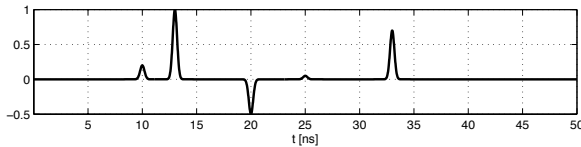
sampling rate: $f_s = 440$ MHz

dynamic range: 26 dB

ADC resolution: 6 bits



Effect of Oversampling



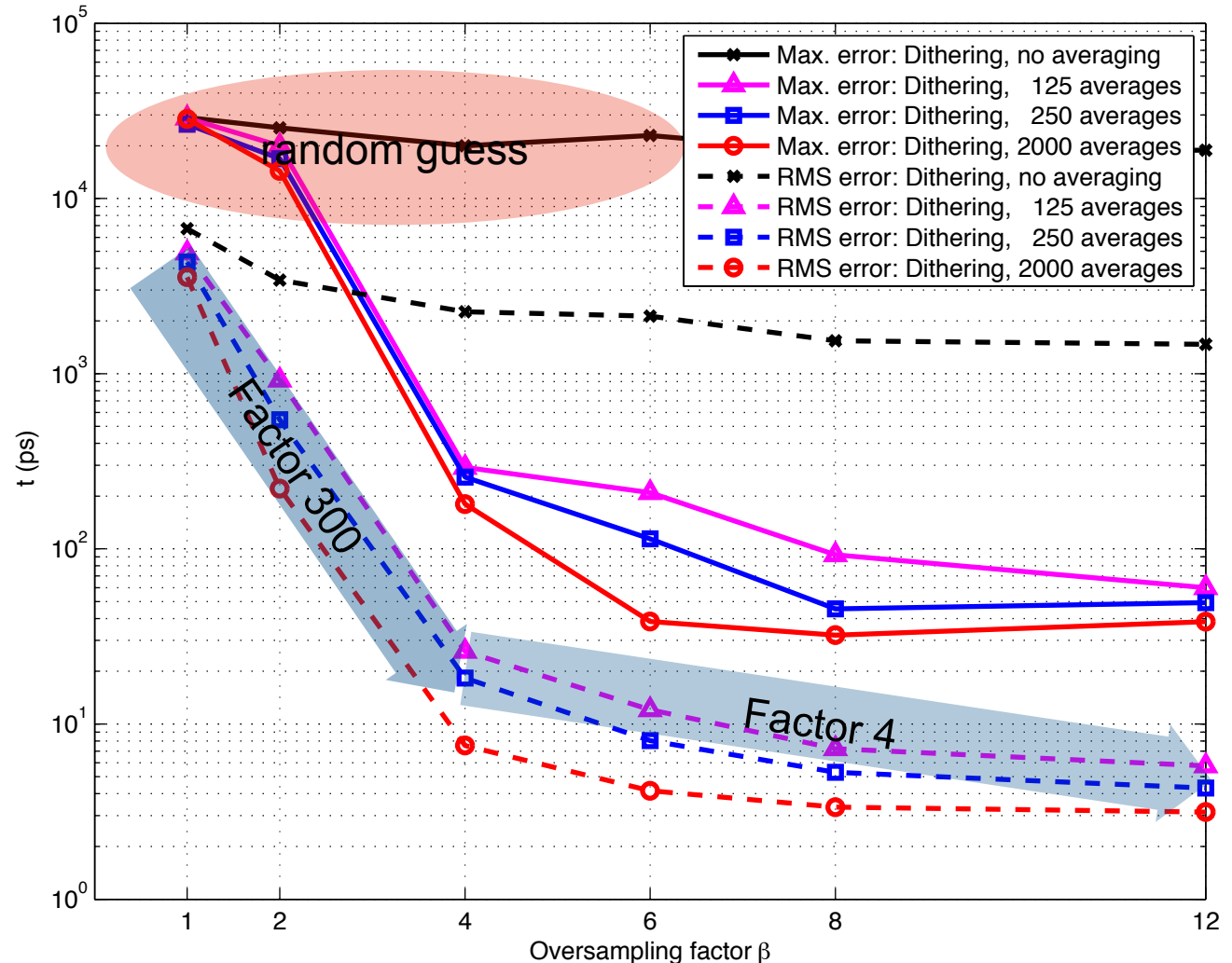
- Oversampling by a factor of 4 enhances the RMSE time resolution by factor of 300.
- An oversampling factor exceeding 12 gives a further improvement by a factor of 4.

Simulation parameters:

sampling rate: $f_s = 440$ MHz

dynamic range: 26 dB

ADC resolution: 6 bits



Conclusions:

- : TDR using FRI is a promising method in respect to efficient hardware implementation.
- : However: TDR using FRI is very sensitive to quantisation noise.
- : Dithering and Averaging leads to significant performance improvements.
- : Improvements are not yet sufficient for highly demanding TDR requirements (<33 ps error).

Outlook:

- : Further reduction of the ToF estimation error is needed.
- : Evaluation of the minimum ToF estimation error bound (Cramer-Rao bound) pending.



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Thank you for your attention.

